

# Boosting heterogeneous VAEs via multi-objective optimization

NeurIPS 2021 Workshop “Your Model is Wrong:  
Robustness and misspecification in probabilistic modeling”

Adrián Javaloy, Maryam Meghdadi, Isabel Valera

University of Saarland  
MPI Software Systems

December 3, 2021

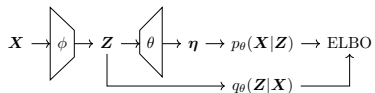


UNIVERSITÄT  
DES  
SAARLANDES

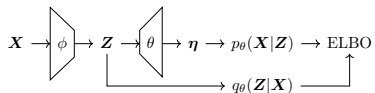


MAX PLANCK INSTITUTE  
FOR SOFTWARE SYSTEMS

# VAEs and heterogeneous data

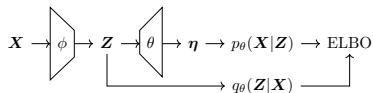


# VAEs and heterogeneous data



$$p_{\theta}(\mathbf{X}|\mathbf{z}) = \prod_{d=1}^D p_d(\mathbf{x}_d|\mathbf{z})$$

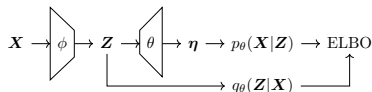
# VAEs and heterogeneous data



$$p_\theta(\mathbf{X}|\mathbf{z}) = \prod_{d=1}^D p_d(\mathbf{x}_d|\mathbf{z})$$

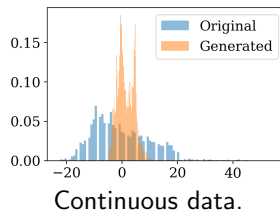
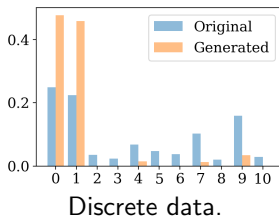
- **Implicit assumption.** We want to learn all features equally well.

# VAEs and heterogeneous data



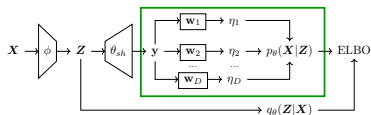
$$p_{\theta}(\mathbf{X}|\mathbf{z}) = \prod_{d=1}^D p_d(\mathbf{x}_d|\mathbf{z})$$

- **Implicit assumption.** We want to learn all features equally well.
- **Problem.** During training, VAEs prioritize some features over others.

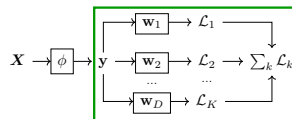


# Multiobjective architectures

## Heterogeneous VAEs

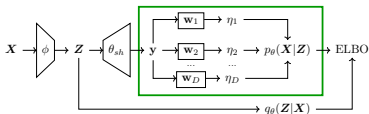


## Multitask Learning



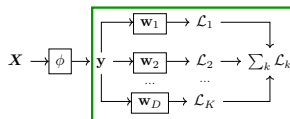
# Multiobjective architectures

## Heterogeneous VAEs



**Want:** Model all features equally well.  
**Problem:** Feature overlooking.

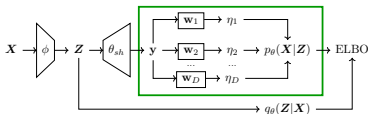
## Multitask Learning



Learn all tasks equally well.  
Negative transfer.

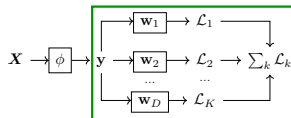
# Multiobjective architectures

## Heterogeneous VAEs



- Want:** Model all features equally well.  
**Problem:** Feature overlooking.  
**Shared:**  $\phi$  and  $\theta_{sh}$ .  
**Exclusive:**  $w_1, w_2, \dots, w_K$ .

## Multitask Learning

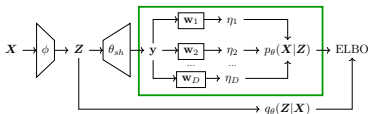


- Learn all tasks equally well.  
Negative transfer.  
 $\phi$ .  
 $w_1, w_2, \dots, w_K$ .



# Multiobjective architectures

## Heterogeneous VAEs

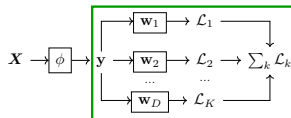


- Want:** Model all features equally well.
- Problem:** Feature overlooking.
- Shared:**  $\phi$  and  $\theta_{sh}$ .
- Exclusive:**  $\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K$ .

**Updating  $\phi$ :**

$$\begin{aligned} \nabla_{\phi} p_{\theta} \nabla_{p_{\theta}} \text{ELBO} &= \\ &= \nabla_{\phi} \mathbf{y} \left( \underbrace{\sum_d \nabla_{\mathbf{y}} \eta_d \nabla_{\eta_d} p_{\theta}}_{\text{feature overlooking}} \right) \nabla_{p_{\theta}} \text{ELBO} \end{aligned}$$

## Multitask Learning

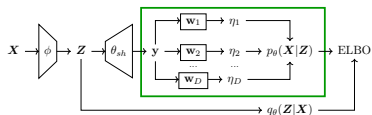


- Learn all tasks equally well.
- Negative transfer.
- $\phi$ .
- $\mathbf{w}_1, \mathbf{w}_2, \dots, \mathbf{w}_K$ .

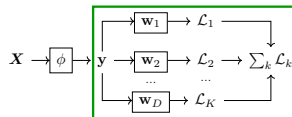
$$\nabla_{\phi} \mathcal{L} = \nabla_{\phi} \mathbf{y} \left( \underbrace{\sum_k \nabla_{\mathbf{y}} \mathcal{L}_k}_{\text{negative transfer}} \right)$$

# Tackling feature overlooking

## Heterogeneous VAEs



## Multitask Learning

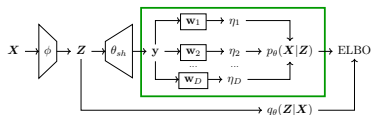


## Conflicting gradients

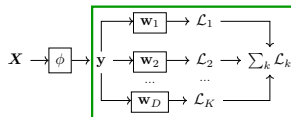
Differences between gradient among tasks/features lead to poor gradient directions, and thus shared-parameters updates.

# Tackling feature overlooking

## Heterogeneous VAEs



## Multitask Learning

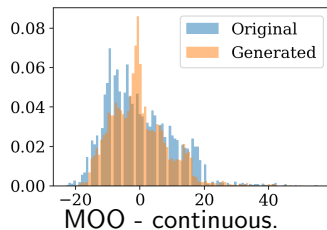
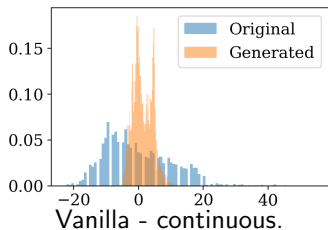
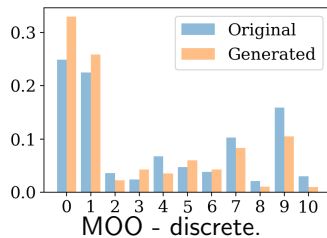
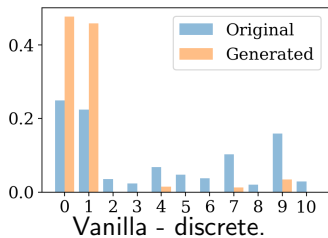


## Conflicting gradients

Differences between gradient among tasks/features lead to poor gradient directions, and thus shared-parameters updates.


These conflicts are restricted to the **green squares**. We can leverage existing MTL solutions to alleviate feature overlooking in heterogeneous VAEs.

# Qualitative results



# Conclusions

- Despite their principled origins, VAEs are not different from other neural models.
- Similar assumptions = similar problems. We can leverage existing solutions.
- If properly trained, VAEs can be incredibly effective at modeling heterogeneous data.

Want to stay tuned?  
Follow us on !



Paper at [adrian.javaloy.com/uploads/movae/ymiw-paper.pdf](https://adrian.javaloy.com/uploads/movae/ymiw-paper.pdf).